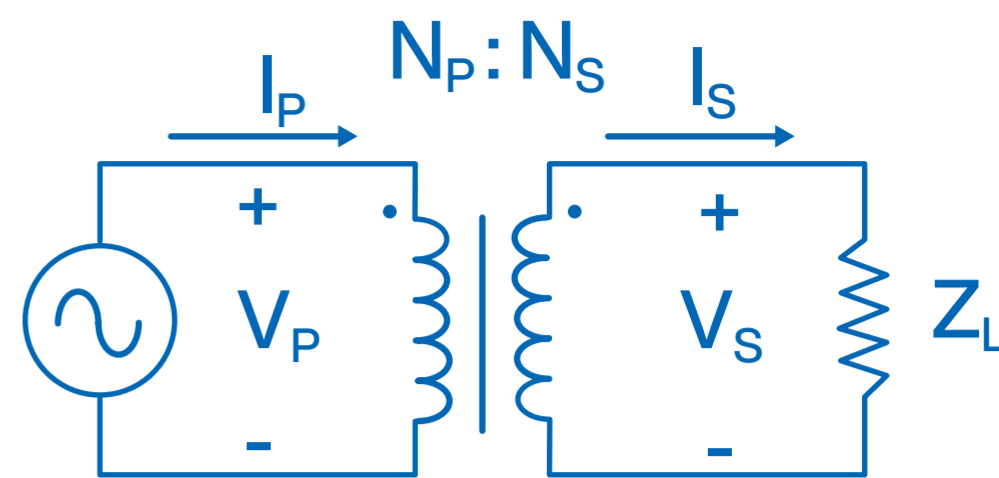


# Transformers Reference Guide

## Transformers

A transformer consists basically of coil windings made of conductive material, surrounding a metal core. A varying current in any one coil of the transformer produces a varying magnetic flux in the transformer's core, which induces a varying electromotive force across other coils. Electrical energy can be transferred between separate coils without a conductive connection between the two circuits.

- Are passive components
- Transfer electrical energy between electrical circuits (coils)
- Obey Faraday's law of induction



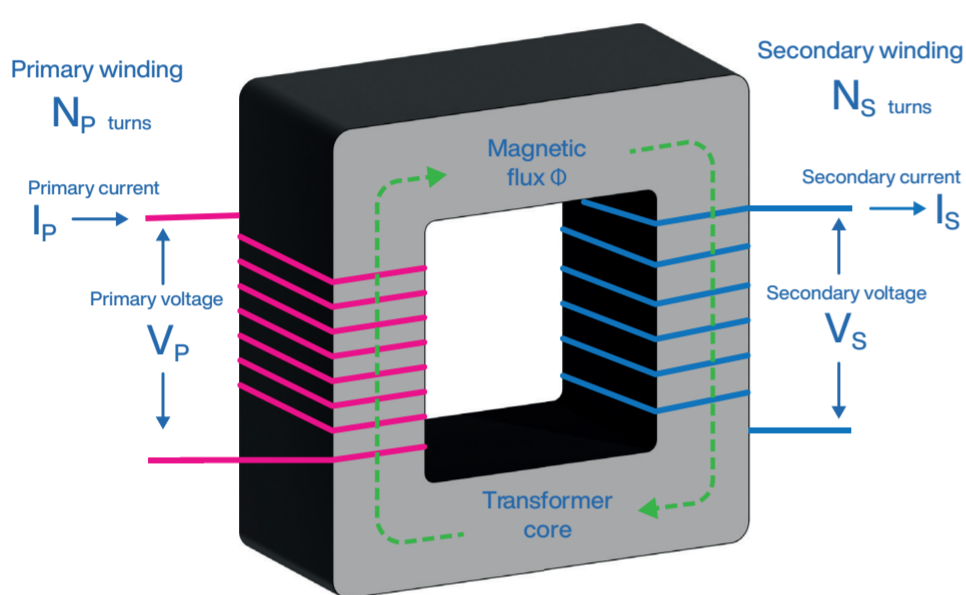
### Key

$N_p$  : Number of windings on primary coil  
 $N_s$  : Number of windings on secondary coil  
 $V_p$  : Instantaneous Voltage on primary coil (source)

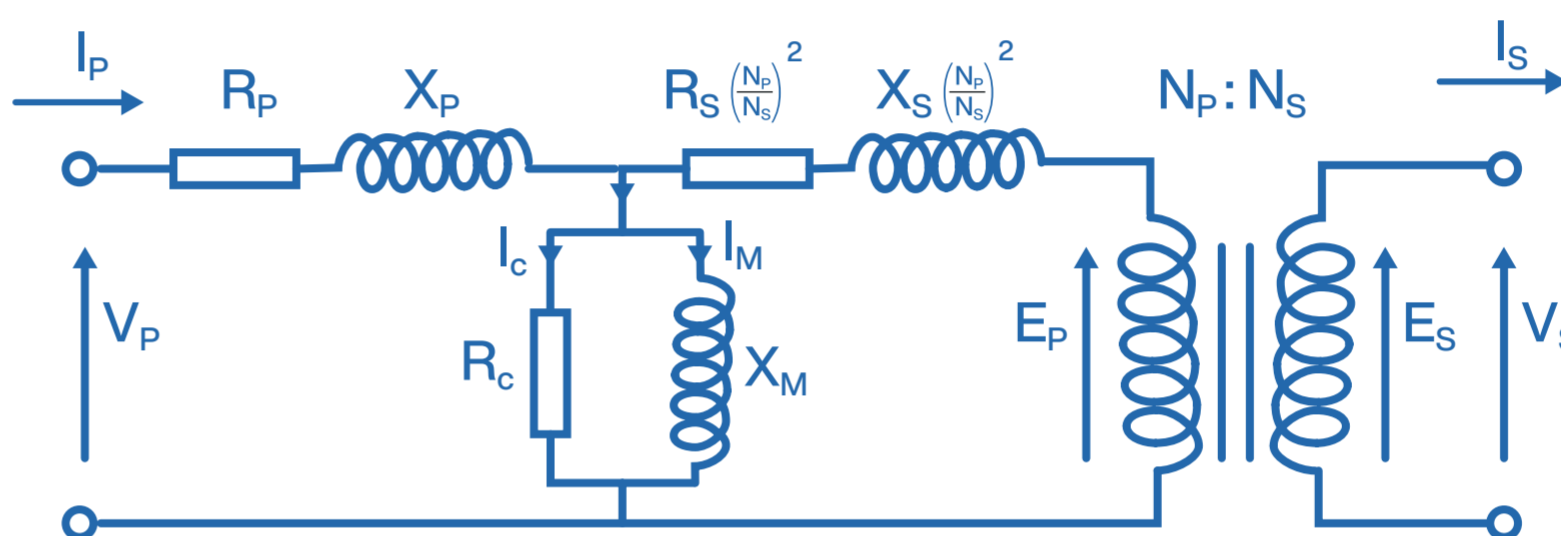
$V_s$  : Instantaneous Voltage on secondary coil  
 $I_p$  : Current on primary coil  
 $I_s$  : Current on secondary coil

$Z_L$  : Load impedance  
 $\Phi$  : Magnetic Flux through one turn of the winding  
 $L$  : Winding self-inductance

## Ideal transformer



Taking these real-world issues into account, the equivalent circuit looks like this:



Winding joule losses and leakage reactances are approximated by loop impedances  $R_p$ ,  $R_s$  and  $X_p$ ,  $X_s$ . Core losses:  $R_c$  and  $X_M$  (magnetizing reactance).

### Equations

$$V_p = -N_p \frac{d\phi}{dt}$$

$$V_s = -N_s \frac{d\phi}{dt}$$

$$\text{Turns ratio } a = \frac{V_p}{V_s} = \frac{N_p}{N_s} = \frac{I_s}{I_p} = \sqrt{\frac{L_p}{L_s}}$$

$a > 1$ : Step-down transformer  
 $a < 1$ : Step-up transformer  
 $a = 1$ : Isolation transformer

### Real-world transformers have to deal with :

#### Core Losses:

- Nonlinear magnetic effects in the core cause Hysteresis Losses
- Heating of the core causes Eddy Current Losses

#### Winding Losses:

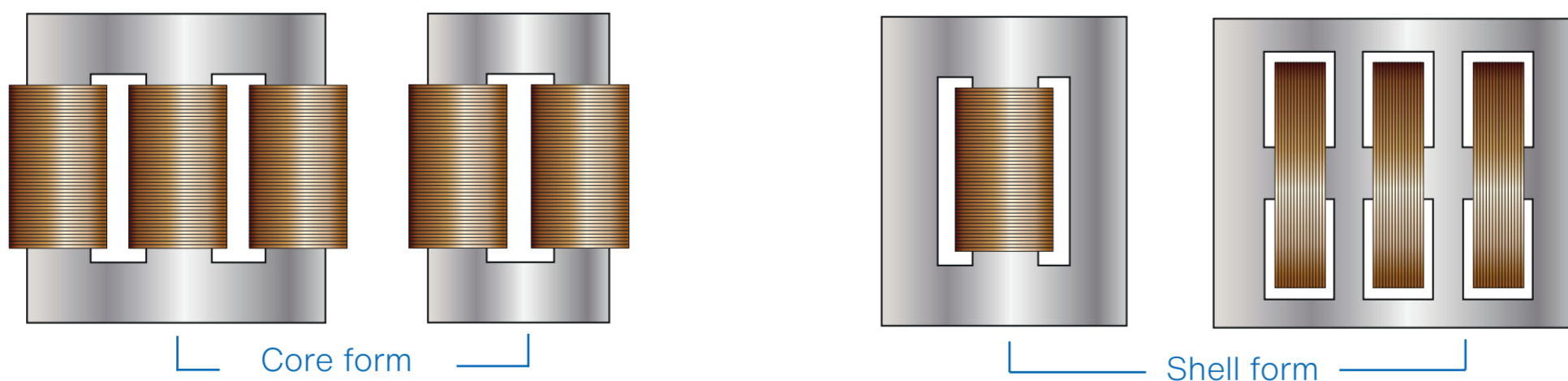
- Resistance and inductance in the winding material cause Joule Losses
- Reactive impedance is caused by leakage flux

#### Parasitic Capacitance:

- Capacitance between adjacent winding layers
- Capacitance between adjacent turns in one winding layer
- Capacitance between Core and adjacent winding layers

## Core Constructions

When windings surround the core, the transformer is **core form**; when windings are surrounded by the core, the transformer is **shell form**.



**Solid Core** - Circuits like switch-mode power supplies that operate above mains frequencies and up to a few tens of kilohertz use powdered iron cores. For higher frequencies, cores made from non-conductive magnetic ceramic materials called ferrites are common.

**Toroidal Core** - Toroidal transformers are constructed around a ring-shaped core, made from a long strip of silicon steel or permalloy wound into a coil, powdered iron, or ferrite.

**Air Core** - Used in RF applications, air core transformers are constructed by placing the windings very close to each other. This design eliminates core losses.

**Laminated Core** - Transformers for use at power or audio frequencies typically have cores made of high permeability silicon steel. The effect of laminations is an enormous reduction of eddy currents.